

# Modeling QTL Effect On BTA6 in Dairy Cattle Using Random Regression Test Day Models

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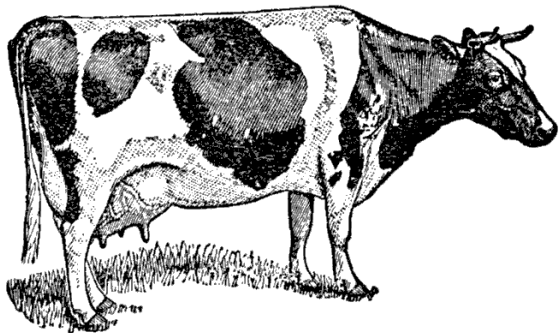
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# Outline

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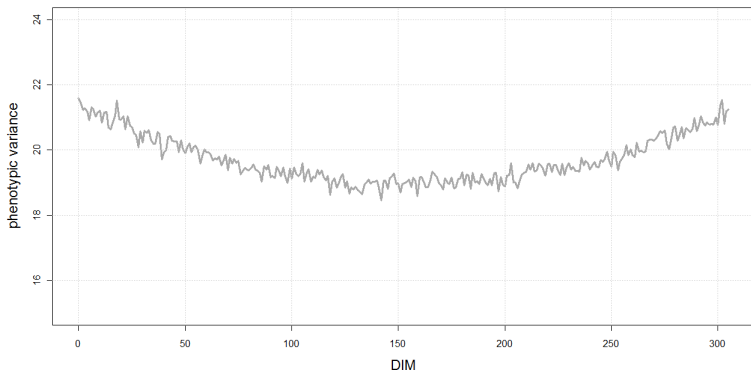
1. Motivation
2. Data Set
3. Methods
4. Results
5. Conclusions



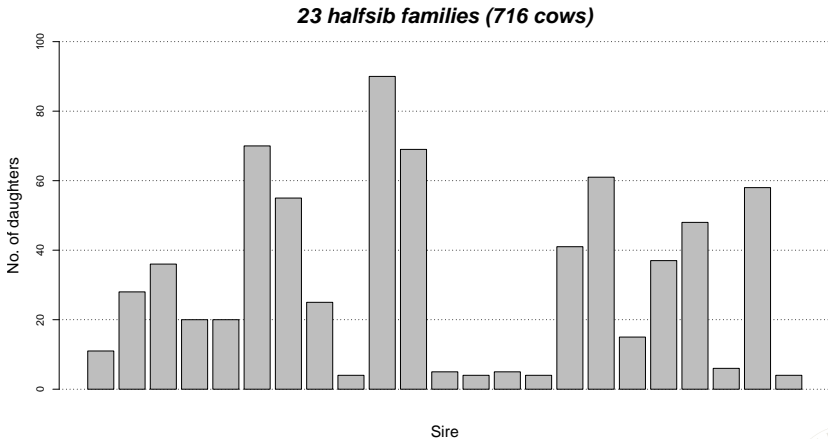
# Main Aim

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- Longitudinal data
  - correlation between observations
  - detection of QTL
  - checking if effects are constant or variable in time



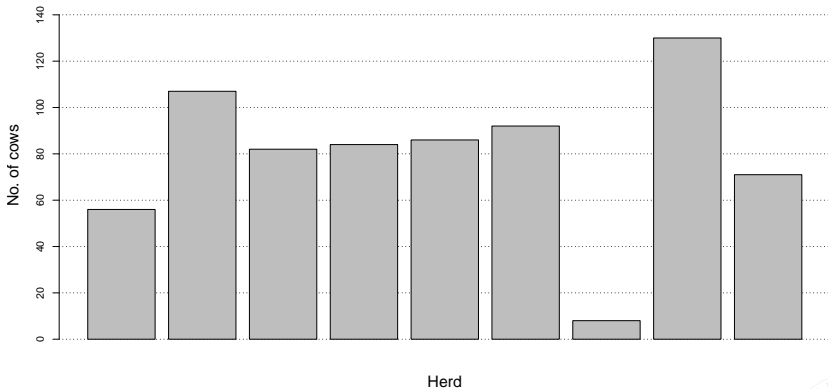
# Material – animals



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## *9 herds*





No.	Marker	Map distance (cM)	Alleles
1	BM1329	0.00	6
2	BMS2508	8.54	7
3	BMS1242	17.44	7
4	BM143	18.33	7
5	BMS518	23.57	4
6	BM4322	28.47	7
7	BMS470	32.00	4
8	ILSTS097	37.04	2
9	RM028	43.79	4
10	BM415	46.56	7
11	ILSTS035	51.87	9
12	ILSTS087	54.34	3
13	BMS2460	58.06	4
14	BP7	63.50	5

# Model 1

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$$y_i = \mu + \beta + \alpha_i + \rho_i + \epsilon_i,$$

where

- $y_i$  – cumulated 305 – day milk yield for cow  $i$
- $\beta$  – fixed effects
- $\alpha_i$  – random additive polygenic effect,  $\alpha \sim \mathcal{N}(0, A\sigma_\alpha^2)$
- $\rho_i$  – random QTL effect,  $\rho \sim \mathcal{N}(0, IBD\sigma_\rho^2)$
- $\epsilon_i$  – residual,  $\epsilon \sim \mathcal{N}(0, I\sigma_\epsilon^2)$



## Model 2

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$$y_{ij} = \beta + \sum_{m=0}^2 \alpha_{im} \phi_m(\tau_{ij}) + \rho_i + \sum_{m=0}^2 \xi_{im} \phi_m(\tau_{ij}) + \epsilon_{ij},$$

where

- $y_{ij}$  –  $j$ th test day record for individual  $i$
- $\phi_m(\tau_{ij})$  –  $m$ th Legendre polynomial at time point  $\tau_{ij}$
- $\alpha_{im}$  –  $m$ th random regression coefficient for additive polygenic effect,  $\alpha \sim \mathcal{N}(0, A \otimes G_\alpha)$
- $\xi_{im}$  –  $m$ th random regression coefficient for permanent environmental effect,  $\xi \sim \mathcal{N}(0, I \otimes P_\xi)$



## Model 3

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$$y_{ij} = \beta + \sum_{m=0}^2 \alpha_{im} \phi_m(\tau_{ij}) + \sum_{m=0}^2 \rho_{im} \phi_m(\tau_{ij}) + \sum_{m=0}^2 \xi_{im} \phi_m(\tau_{ij}) + \epsilon_{ij},$$

where

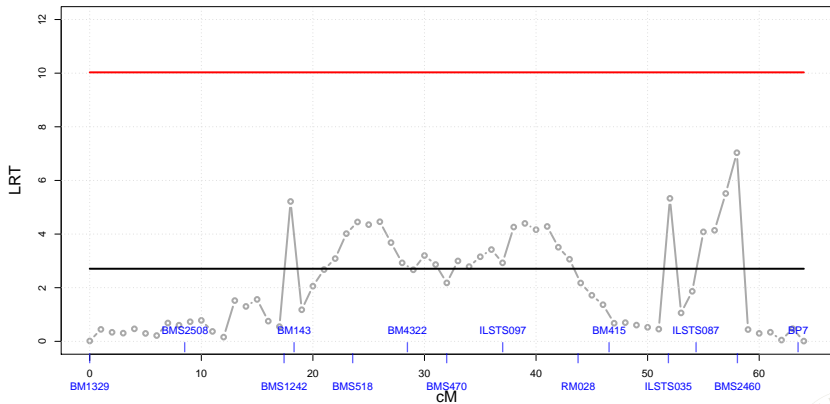
- $\rho_{im}$  –  $m$ th random regression coefficient for QTL effect,  
 $\rho \sim \mathcal{N}(0, IBD \otimes G_\rho)$

$$\begin{aligned} -2 \log L &= \text{const} + n \log \sigma_\epsilon^2 + 3 \log |A| + N \log |G_\alpha| + 3 \log |IBD| \\ &+ N \log |G_\rho| + N \log |P_\xi| + \log |C| + y^T S y \end{aligned}$$



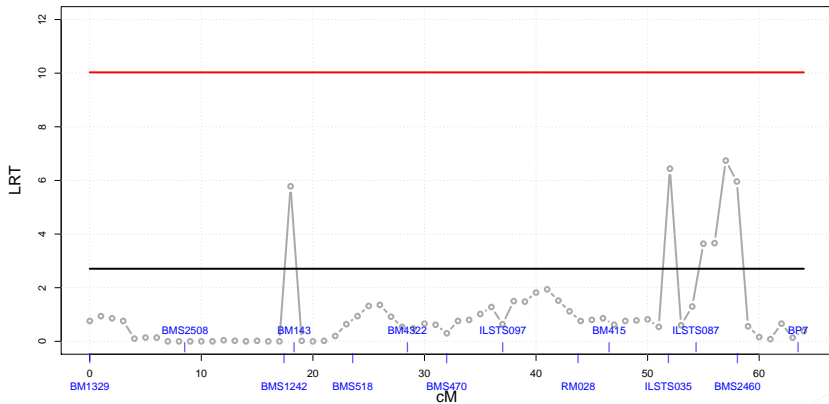
# Results – Model 1

$$H_0: \sigma_p^2 = 0 \text{ vs. } H_1: \sigma_p^2 > 0$$



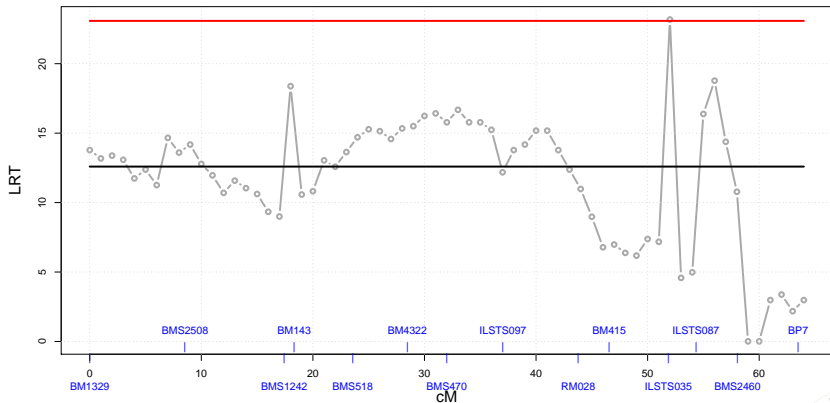
## Results – Model 2

$$H_0: \sigma_p^2 = 0 \text{ vs. } H_1: \sigma_p^2 > 0$$



## Results – Model 3

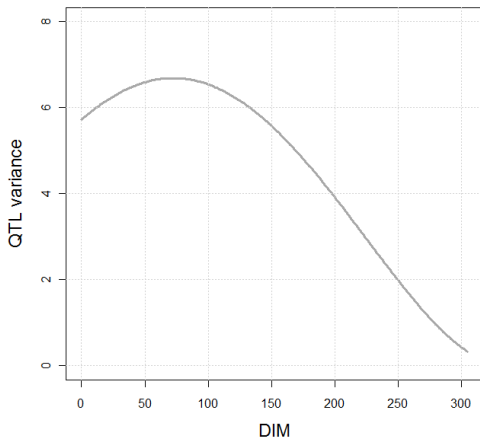
$H_0 : G_p=0$  vs.  $H_1 : G_p$  is positive definite



## Results – Significant QTL (52 cM)

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$$q_i = \Phi(\tau_i)G_\rho\Phi^T(\tau_i), \quad \text{where} \quad \Phi(\tau_i) = [\phi_0(\tau_i), \phi_1(\tau_i), \phi_2(\tau_i)]^T$$



## Conclusions

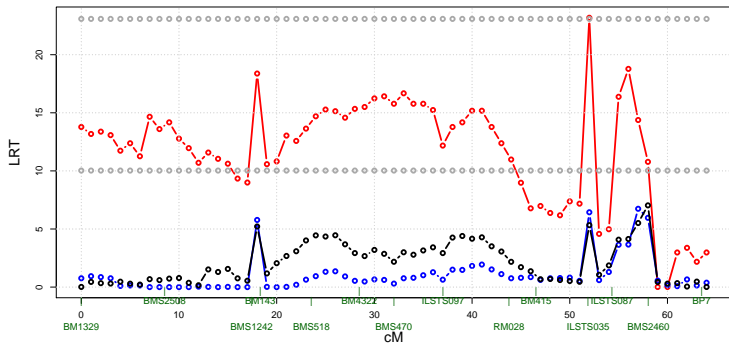
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- Using Bonferroni correction we were able to detect only QTL at 52 cM (between markers ILST035 – ILST087).
- The other are only suggestive QTL (near markers BM143 and BMS2460 and between markers BM4322 and ILST097).
- All QTL have been reported in previous works (Spelman et al. 1996, Zhang et al. 1998 and Nadesalingam et al. 2001).
- It can be assumed that QTL effect (significant QTL) is variable in time.



# Conclusions

- Position of the QTL was similar by all models, but model 3 (red line) provided the highest significance despite more parameters and thus higher critical value.



# Thank You!

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